

# Detector rate sensitivity to Beam position, angle, energy

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- Produce plots of tile rate sensitivities to beam energy scan with  $\pm 110$  MeV shifts.
- Replotted tile rate sensitivities with each tile's azimuthal scattering angle  $\phi_{acc}$  instead of geometric  $\phi$
- Fix the error bars on  $S_r$ ,  $S_t$ , dipole response distributions

# Simulation Setup

- remoll Geant4 — develop branch, commit 2bb7397 + PR640 (coll2redesign)
- Moller + ep-elastic generators
- Scan five beam parameters independently:  
 $pos_X, pos_Y, angle_X, angle_Y, Energy$
- Selected events with  $e^\pm, \pi^\pm$ ,  $k > 1$  MeV
- Calculated

$$\text{Fractional sensitivity} = \frac{1}{R_0} \frac{dR}{dX}$$

where  $X \in$

$\{pos_X, pos_Y, angle_X, angle_Y, Energy\}$

Scan	Range	Unit
$pos_X$	$\pm 1$	mm
$pos_Y$	$\pm 1$	mm
$angle_X$	$\pm 0.2$	mrad
$angle_Y$	$\pm 0.2$	mrad
energy	$\pm 110$	MeV

- nominal beam energy,  $E_0 = 11$  GeV, scan corresponds to  $\Delta E/E = \pm 10^{-2}$
- 6 rings, 28 segments,
- Ring 5 split L/C/R tiles
- 224 ring detector tiles

## $\phi_{\text{acc}}$ : definition

- Used two remoll output branches: `hit` (every detector hit in the event) and `part` (every primary particle in the event). They are linked by a track ID.
- In order to find the primary that produced a given hit, we match `hit.trid` with `part.trid` and get `part.ph`: the lab-frame azimuthal angle of primary particle. We call this  $\phi_{\text{acc}}$ , in contrast to  $\phi_{\text{geom}}$ , the geometric center of the tile.
- `part.ph` is in radians in the range  $(-\pi, \pi]$ . For each generator (Moller, elastic), the per-tile circular mean is computed from all accepted tracks  $i$  with rate weights  $w_i$ :

$$\bar{\phi}_{\text{gen}} = \text{atan2}\left(\sum_i w_i \sin \phi_i, \sum_i w_i \cos \phi_i\right), \quad R_{\text{gen}} = \sum_i w_i.$$

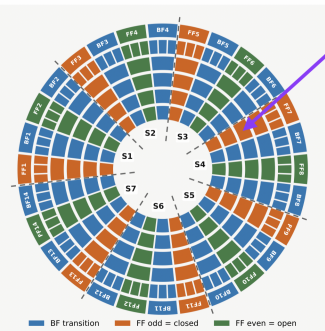
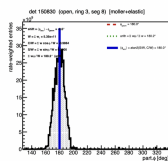
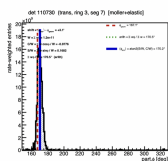
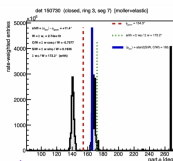
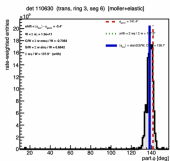
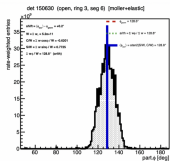
- Then, two generators are combined into a single rate-weighted circular mean per tile:

$$C = R_{\text{mol}} \cos \bar{\phi}_{\text{mol}} + R_{\text{el}} \cos \bar{\phi}_{\text{el}}, \quad S = R_{\text{mol}} \sin \bar{\phi}_{\text{mol}} + R_{\text{el}} \sin \bar{\phi}_{\text{el}},$$

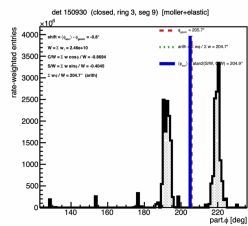
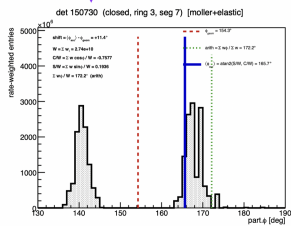
$$\langle \phi_{\text{acc}} \rangle = \text{atan2}(S, C).$$

- This  $\langle \phi_{\text{acc}} \rangle$  is what I use as the x-axis of each tile in the  $S$ -vs- $\phi$ ,  $S_r$ ,  $S_t$ , and dipole plots, in place of  $\phi_{\text{geom}}$ .

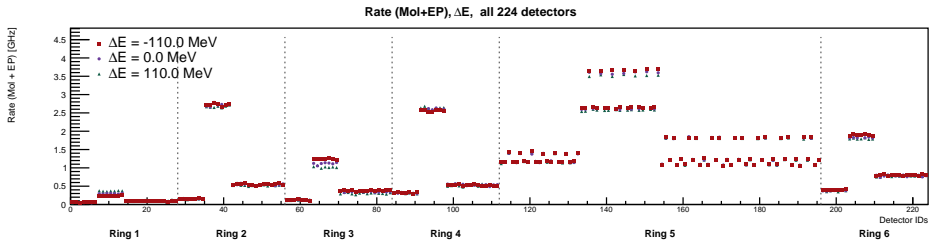
# $\phi_{acc}$ : definition



**Zoomed-in**

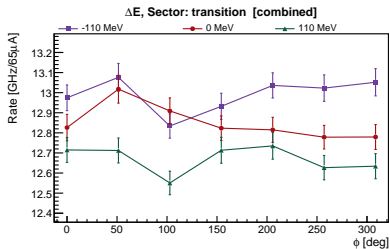
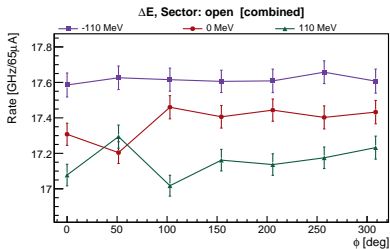
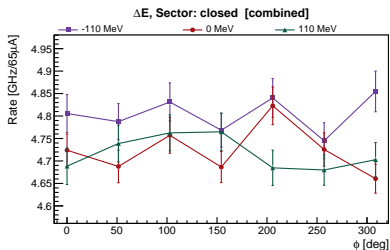
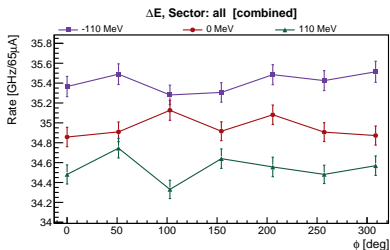


# Detector rate as a function of tile ID, energy scans



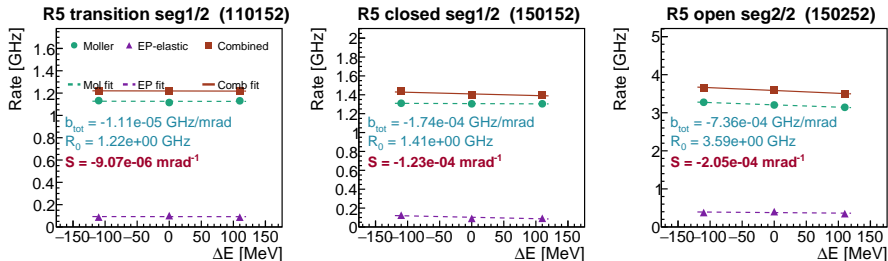
Combined rate for nominal,  $\pm 110$  MeV shifts.

# Septant summed detector rates, energy scan



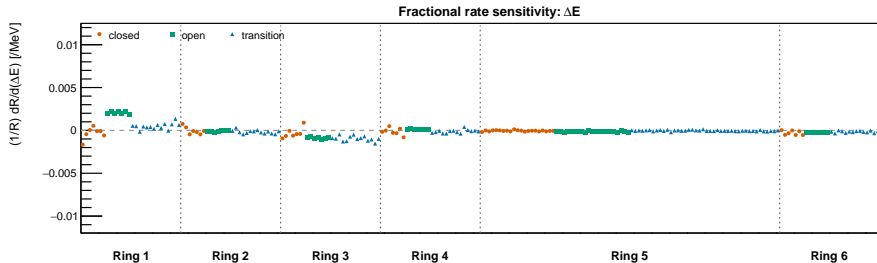
Each point is the sum of rates over all tiles in that septant, grouped by tile type (closed/open/-transition).

# Detector rate as a function of beam energy scan



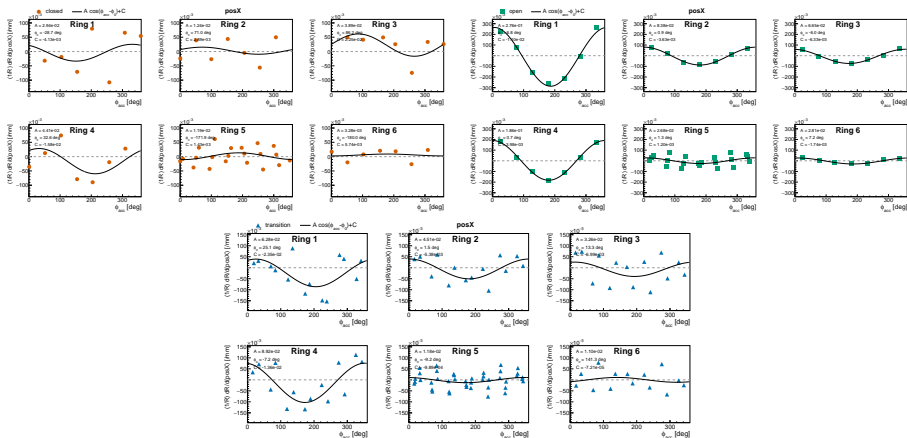
rate vs  $\Delta E$  for selected tiles in transition/closed/open sector.

# Fractional sensitivity as a function of detector ID, energy scans



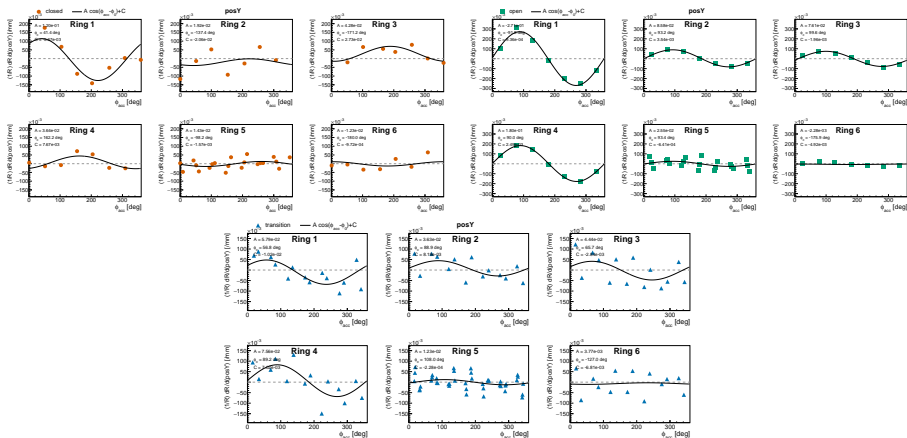
$S = b_{\text{tot}}/R_0$  per tile. Tiles ordered by ring; within each ring: closed, open, transition.

# Fractional sensitivity ( $pos_X$ scan) as a function of azimuthal scattering angle $\phi$



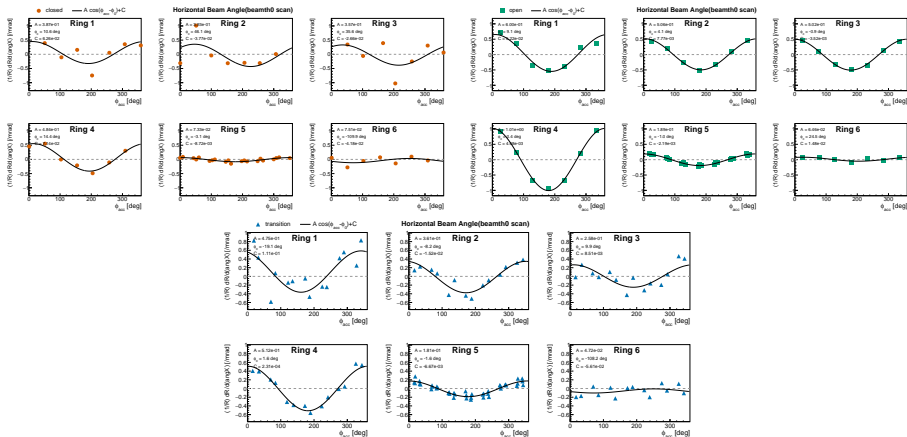
Fractional sensitivity vs azimuthal scattering angle  $\phi$  for each ring. posX shows  $\cos\phi$  dependence.

# Fractional sensitivity ( $pos_Y$ scan) as a function of azimuthal scattering angle $\phi$



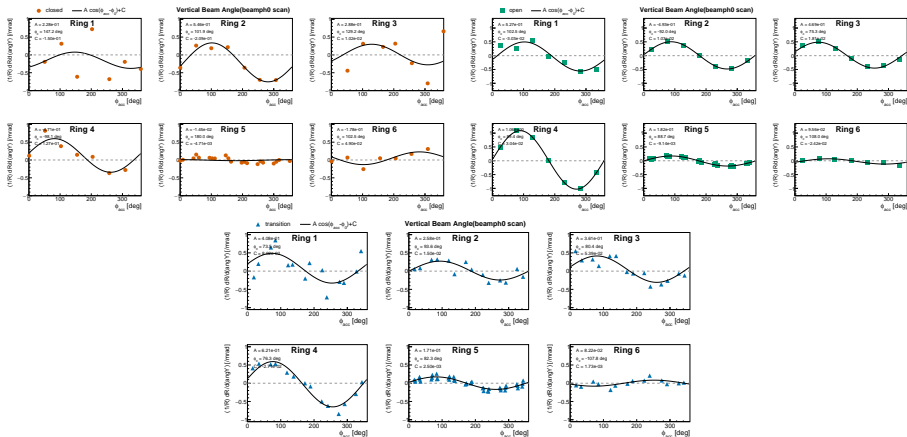
Fractional sensitivity vs azimuthal scattering angle  $\phi$  for each ring. posY shows  $\sin\phi$  dependence.

# Fractional sensitivity ( $ang_X$ scan) as a function of azimuthal scattering angle $\phi$



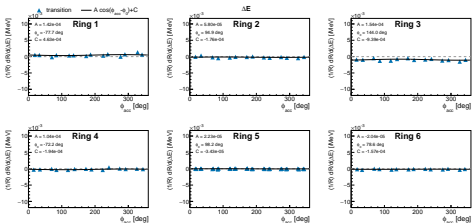
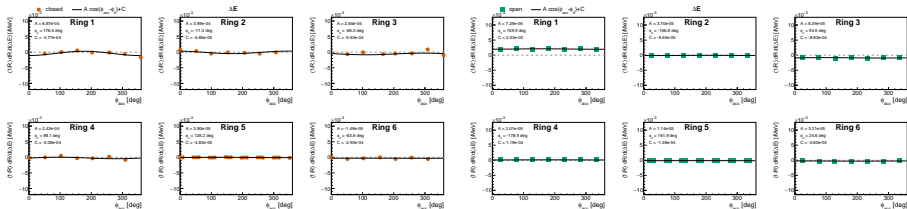
Fractional sensitivity vs azimuthal scattering angle  $\phi$  for each ring.  $ang_X$  shows  $\cos\phi$  dependence.

# Fractional sensitivity ( $ang_Y$ scan) as a function of azimuthal scattering angle $\phi$



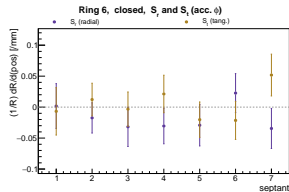
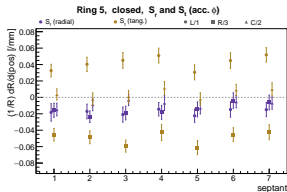
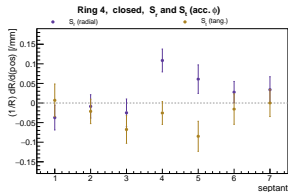
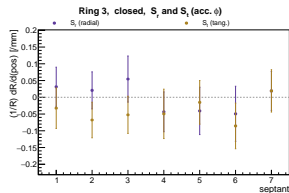
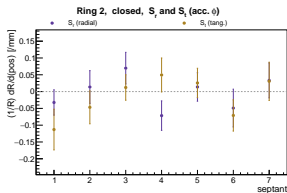
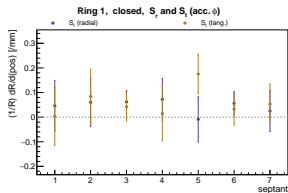
Fractional sensitivity vs azimuthal scattering angle  $\phi$  for each ring.  $ang_Y$  shows  $\sin\phi$  dependence.

# Fractional sensitivity (energy scan) as a function of azimuthal scattering angle $\phi$



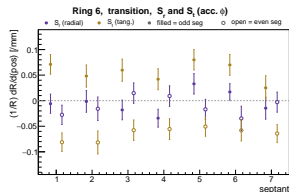
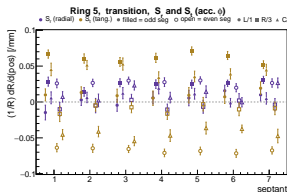
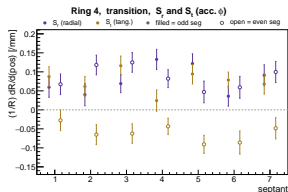
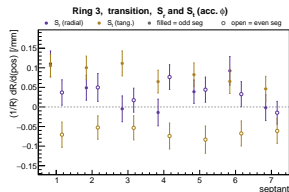
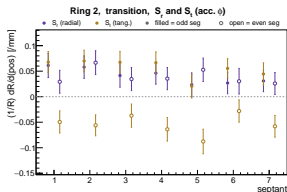
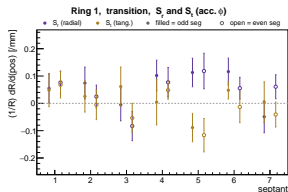
Fractional sensitivity vs azimuthal scattering angle  $\phi$  for each ring. The curves are flat, shows that beam energy has no  $\phi$  dependence.

# $S_r$ and $S_t$ , position sensitivity, closed



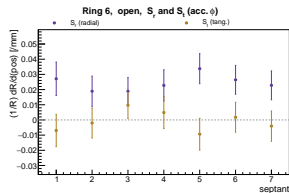
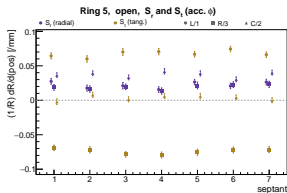
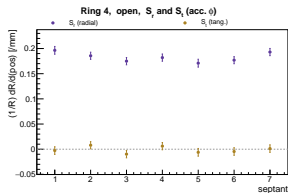
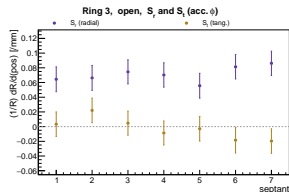
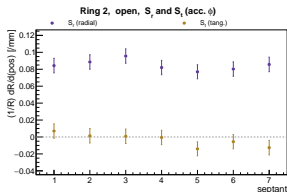
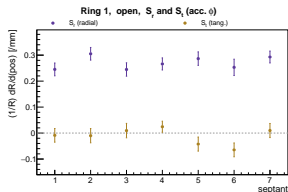
$S_r$  and  $S_t$  [ $mm^{-1}$ ] from position scans, per tile, grouped by closed sectors and rings.

# $S_r$ and $S_t$ , position sensitivity, transition



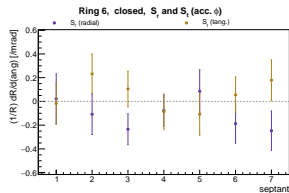
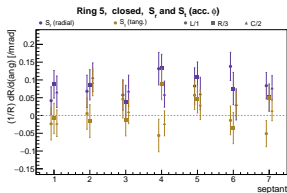
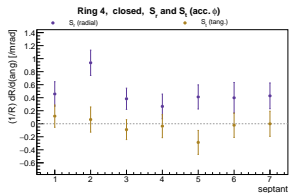
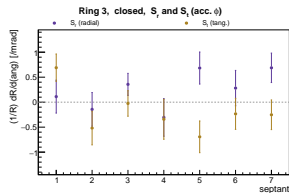
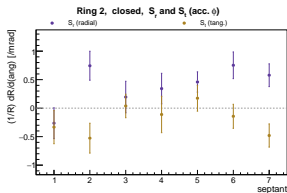
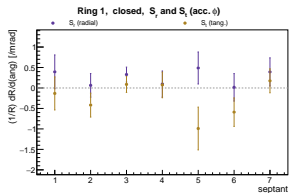
$S_r$  and  $S_t$  [ $mm^{-1}$ ] from position scans, per tile, grouped by transition sectors and rings.

# $S_r$ and $S_t$ , position sensitivity, open



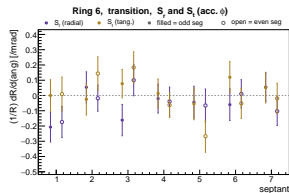
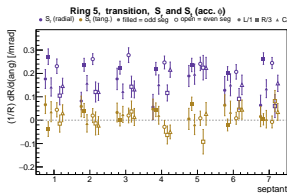
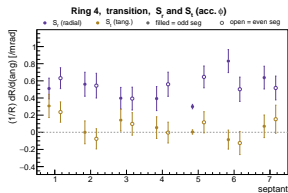
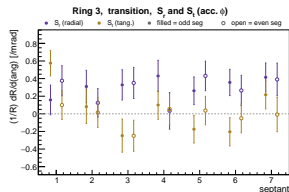
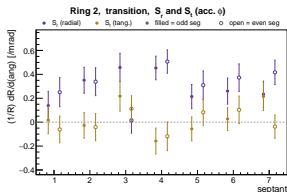
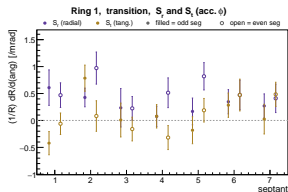
$S_r$  and  $S_t$  [ $mm^{-1}$ ] from position scans, per tile, grouped by open sectors and rings.

# $S_r$ and $S_t$ , angle sensitivity, closed



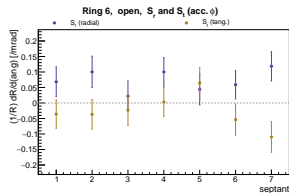
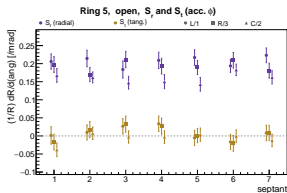
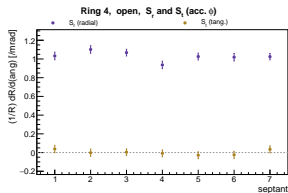
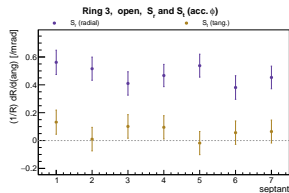
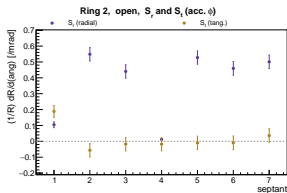
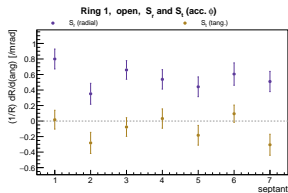
$S_r$  and  $S_t$  [ $mrad^{-1}$ ] from angle scans, per tile, grouped by closed sectors and rings.

# $S_r$ and $S_t$ , angle sensitivity, transition



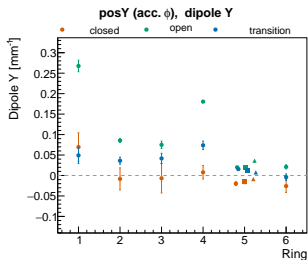
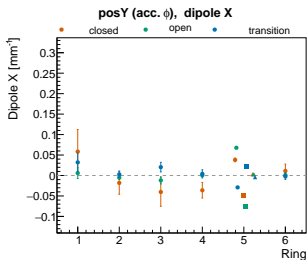
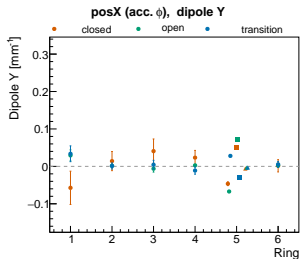
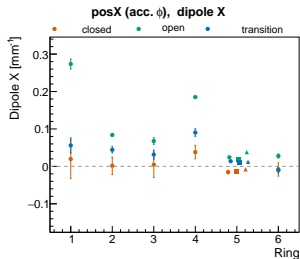
$S_r$  and  $S_t$  [ $\text{mrad}^{-1}$ ] from angle scans, per tile, grouped by transition sectors and rings.

# $S_r$ and $S_t$ , angle sensitivity, open



$S_r$  and  $S_t$  [ $\text{mrad}^{-1}$ ] from angle scans, per tile, grouped by open sectors and rings.

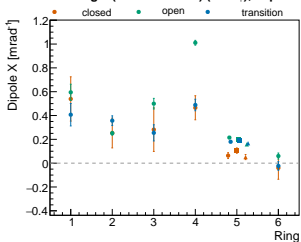
# Dipole response, position scans



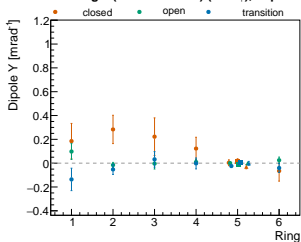
$D_x$  and  $D_y$  from position scans, per tile, grouped by open/closed/transition sectors and rings.

# Dipole response, angle scans

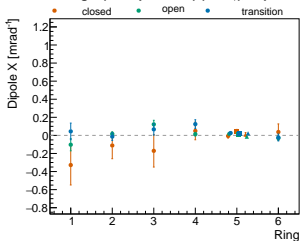
Horizontal Angle (beamth0 scan) (acc.  $\phi$ ), dipole X



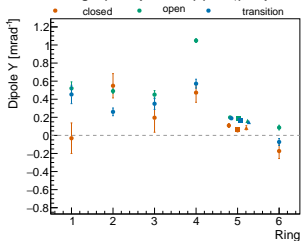
Horizontal Angle (beamth0 scan) (acc.  $\phi$ ), dipole Y



Vertical Angle (beamph0 scan) (acc.  $\phi$ ), dipole X



Vertical Angle (beamph0 scan) (acc.  $\phi$ ), dipole Y



$D_x$  and  $D_y$  from angle scans, per tile, grouped by open/closed/transition sectors and rings.

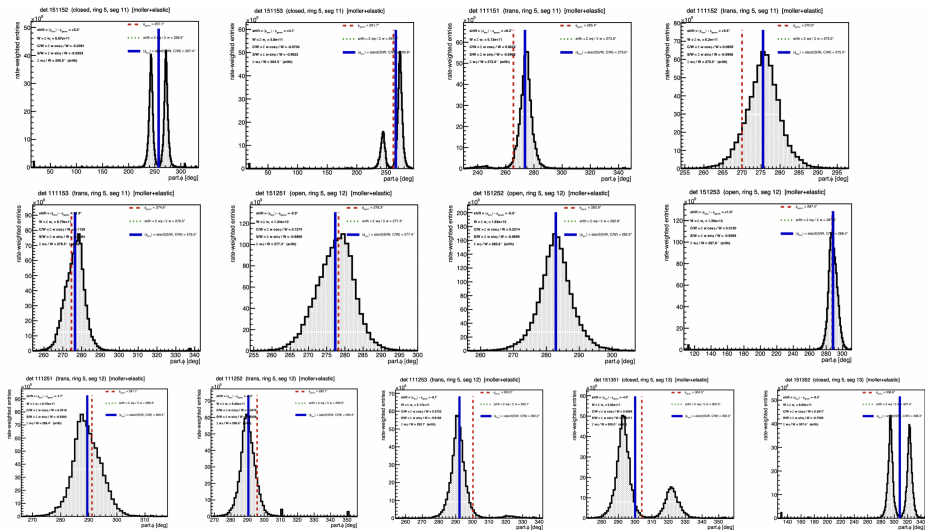
# Mock data sensitivity parameters

Generated mock\_parameters\_thinqtz\_remoll.map for japan-MOLLER mock data generator, replacing placeholder sensitivities with remoll simulation values.

- NormRate (Hz/ $\mu$ A), VoltPerHz, Asym columns are unchanged.
- $C_x$ ,  $C_y$ : position sensitivities  $S_{posX}$ ,  $S_{posY}$  in ppm/nm = mm<sup>-1</sup>
- $C_{xp}$ ,  $C_{yp}$ : angle sensitivities  $S_{angX}$ ,  $S_{angY}$  in ppm/nrad = mrad<sup>-1</sup>
- $C_e$ : energy sensitivity =  $S_{beamE} [MeV^{-1}] \times E_{beam} [MeV]$ , converting from per-MeV to per-fractional-energy ( $\times 11000$ )

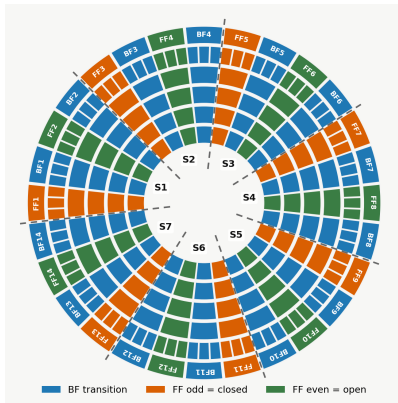
	!Name	NormRate(Hz/uA)	VoltPerHz	Asym	C_x	C_y	C_xp	C_yp	C_e
1	TQ01_R1	110923	2.120e-07	0.0001	0.065151	-0.010319	0.302114	0.383741	-18.454511
2	TQ01_R2	1144615	4.120e-08	0.0001	-0.022958	-0.134693	-0.259057	-0.332105	5.688359
3	TQ01_R3	756923	4.120e-08	0.0001	0.024577	-0.016492	0.021176	0.659107	-10.392786
4	TQ01_R4	2553846	1.140e-08	0.0001	-0.032218	-0.000421	0.459242	0.107991	-1.887232
5	TQ01_R5C	20307692	8.420e-10	0.0001	-0.015643	0.003089	0.050700	-0.017208	-0.1328196
6	TQ01_R5L	17230769	2.530e-09	0.0001	-0.016734	0.036369	0.049239	-0.029879	-2.119375
7	TQ01_R5R	17076923	2.530e-09	0.0001	-0.008074	-0.047233	0.090440	0.001709	-0.148755
8	TQ01_R6	4169230	1.140e-08	0.0001	0.018375	-0.009820	0.039895	-0.042554	0.188172
9	TQ02_R1	375384	4.120e-08	0.0001	0.041545	0.058629	0.007687	-0.174455	3.318377
10	TQ02_R2	6030769	2.530e-09	0.0001	0.032854	0.073930	0.175586	0.046817	0.053490
11	TQ02_R3	3569230	1.140e-08	0.0001	0.063188	0.120228	-0.042144	0.546044	-10.711804
12	TQ02_R4	4230769	1.140e-08	0.0001	0.033616	0.093168	0.393296	0.416491	-2.759462
13	TQ02_R5C	18615384	8.420e-10	0.0001	-0.007894	0.044808	0.127638	0.063811	-0.129591
14	TQ02_R5L	15538461	2.530e-09	0.0001	-0.019304	0.006014	0.146576	0.095076	0.066807
15	TQ02_R5R	26307692	8.420e-10	0.0001	0.002864	0.071097	0.257897	0.054749	-0.675243
16	TQ02_R6	11292307	2.530e-09	0.0001	-0.025619	0.073679	-0.202410	-0.053933	-1.562488
17	TQ03_R1	1723076	1.140e-08	0.0001	0.225852	0.100883	0.648281	0.353843	21.373926
18	TQ03_R2	39076923	8.420e-10	0.0001	0.073477	0.039863	0.442524	0.211708	-0.446170
19	TQ03_R3	16615384	2.530e-09	0.0001	0.056354	0.038470	0.476039	0.375052	-9.647679
20	TQ03_R4	35384615	8.420e-10	0.0001	0.180643	0.082172	0.940339	0.491900	1.280232
21	TQ03_R5C	54923076	8.420e-10	0.0001	0.033010	0.013191	0.163707	0.039085	-2.281362
22	TQ03_R5L	40307692	8.420e-10	0.0001	0.003915	0.069600	0.188247	0.074560	-1.949280
23	TQ03_R5R	40307692	8.420e-10	0.0001	0.051894	-0.049028	0.180948	0.087607	-1.412514
24	TQ03_R6	29230769	8.420e-10	0.0001	0.028126	0.003472	0.081620	-0.003981	-2.290296

# Backup



# Quartz tiles

- Tiles are split into **6 rings** (Ring 1 = innermost, Ring 6 = outermost).
- Within each ring, tiles are in this fixed order:
  - **Closed** FF-odd segments (1, 3, 5, 7, 9, 11, 13)
  - **Open** FF-even segments (2, 4, 6, 8, 10, 12, 14)
  - **Transition** BF, all segments (1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14)



# How is the fractional sensitivity calculated?

- Run 3 simulations:  $X = -1$  mm, 0 (nominal),  $+1$  mm (or  $\pm 0.2$  mrad for angles, or  $\pm 110$  MeV for energy).
- Extract detector hit rate  $R_d(X)$  [GHz] from the simulation output.
- Fit a straight line through those 3 points:

$$R_d(X) = \underbrace{a_d}_{\approx R_0} + \underbrace{b_d}_{\text{slope}} \cdot X$$

$b_d = dR_d/dX$  in GHz/mm (or GHz/mrad, GHz/MeV).

- Both generators' slopes and nominal rates are summed:  
 $b_d^{\text{tot}} = b_d^{\text{Mol}} + b_d^{\text{EP}}$ ,  $a_d^{\text{tot}} = a_d^{\text{Mol}} + a_d^{\text{EP}}$
- Divide slope by the rate at  $X = 0$  (the fit intercept  $a_d$ ):

$$\frac{1}{R_0} \frac{dR}{dX} = \frac{b_d^{\text{tot}}}{a_d^{\text{tot}}}$$

## Sensitivity depends on azimuthal angle $\phi$

- a horizontal beam shift ( $x$ ) will cause a left-right asymmetry in the detector response, so the sensitivity to  $x$  will vary with  $\phi$  (max at  $\phi = 0^\circ$ , min at  $\phi = 180^\circ$ )
- a vertical beam shift ( $y$ ) will cause an up-down asymmetry, so the sensitivity to  $y$  will also vary with  $\phi$  (max at  $\phi = 90^\circ$ , min at  $\phi = 270^\circ$ )
- in order to remove the  $\phi$  dependence, we can rotate the sensitivities into a local basis for each tile.

# Rotated basis and dipole response

For each tile, we use its azimuthal angle to convert the X and Y sensitivities into that tile's own local coordinates;

$$S_r = \cos \phi S_x + \sin \phi S_y \quad S_t = -\sin \phi S_x + \cos \phi S_y$$

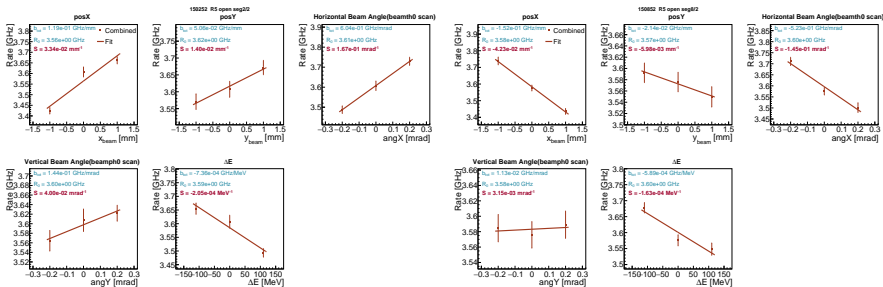
- $S_r$ : radial sensitivity,  $S_t$ : tangential sensitivity
- This rotation is applied separately to position ( $S_{posX}, S_{posY}$ ) and angle ( $S_{angX}, S_{angY}$ ) scans.
- here, azimuthal angle  $\phi$  is geometric center of each tile.
  - FF tiles at  $\phi = (n-1) \times 360^\circ/14$ ,
  - BF tiles offset by  $360^\circ/28$  ( $\approx 12.86^\circ$ ), where  $n$  is the segment number (1-14).
  - Ring 5 subtiles offset from segment center by  $\pm 4.59^\circ$  (L, R).

Then, for a given ring and tile type, the dipole is computed from N tiles around azimuth;

$$D_x = \frac{2}{N} \sum_k S(\phi_k) \cos \phi_k \quad D_y = \frac{2}{N} \sum_k S(\phi_k) \sin \phi_k$$

- $S(\phi_k)$ : fractional sensitivity of tile k for a given scan (posX, angX, etc.).
- $D_x$  and  $D_y$ : horizontal and vertical dipole response.

# All scan comparison



rate vs scan value for all 5 scans, for two selected tiles 150252 (left), 150852 (right).